

DESIGN OF HYBRID APPROXIMATE ADDERS FOR ENERGY-EFFICIENT
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Abstract : Adders are one of the most widely digital components in the digital integrated circuit design and are the necessary part of Digital Signal Processing (DSP) applications. With the advances in technology, researchers have tried and are trying to design adders which offer either high speed, low power consumption, less area or the combination of them. In this paper, the design of various adders such as Simple yet Accuracy Reconfigurable adders are discussed and the performance parameters of adders such as area and delay are determined and compared. Various adders are designed using Verilog in Virtex-6 FPGA devices. Then, they are simulated and synthesized using Xilinx ISE 14.2 for Virtex-6 family device with speed grade -2.

Keywords : Ripple Carry Adder; Carry Skip Adder; Carry Increment Adder; Carry Look Ahead Adder; Carry Save Adder; Carry Select Adder; Carry Bypass Adder.

I. INTRODUCTION

In Arithmetic unit are the essential blocks of digital systems such as Digital Signal Processor (DSP), microprocessors, microcontrollers, and other data processing units. Adders become a critical hardware unit for the efficient implementation of arithmetic unit. In many arithmetic applications and other kinds of applications, adders are not only in the arithmetic logic unit, but also in other parts of processor. Addition operation can also be used in complement operations (1's, 2's, and so on), encoding, decoding and so on. In general, addition is a process which involves two numbers which are added and carry will be generated. The addition operations will result in sum value and carry value. All complex adder architectures are constructed from its basic building blocks such as Half Adder (HA) and Full Adder (FA). In this paper, an attempt has been made to design and simulate the different types of adders using Verilog language and Xilinx ISE 14.2. Then the performance parameters of the various adders are calculated and compared. The rest of the paper is organized as follows: Section I deals with the introduction about adders. In section II, the designs and the features of various adders are discussed. And section III deals with the simulation and synthesis results of adders.

II. EXISTING METHOD

2.1 Approximate Adders

we consider in this study the exploration of the fifth approximate version of AMA [13] and the Error-Tolerant Adder I [11], because they are also explored by related works [22], [23]. The former approximate adder is renamed to "Copy adder" due to its copy function implemented by the buffers. The approximate adders which are explored in this study can be observed in Figure 1. The "Copy adder" in Figure 1(a) has its k bits long approximate part implemented by buffers to copy the operand a to the sum. This procedure has 50% probability of getting the correct sum for each bit position. Furthermore, the carry-in estimation for the precise part is implemented by the more straightforward assignment of the input operand bit b_{k-1} . This procedure has 75% probability of getting a correct carry-in estimation to the precise block. The use of half adders implements the approximate part of the ETAI in Figure 1(b). The sum is performed in the non-conventional direction, (i.e. from the most significant bit $k-1$ to the least significant bit position 0).

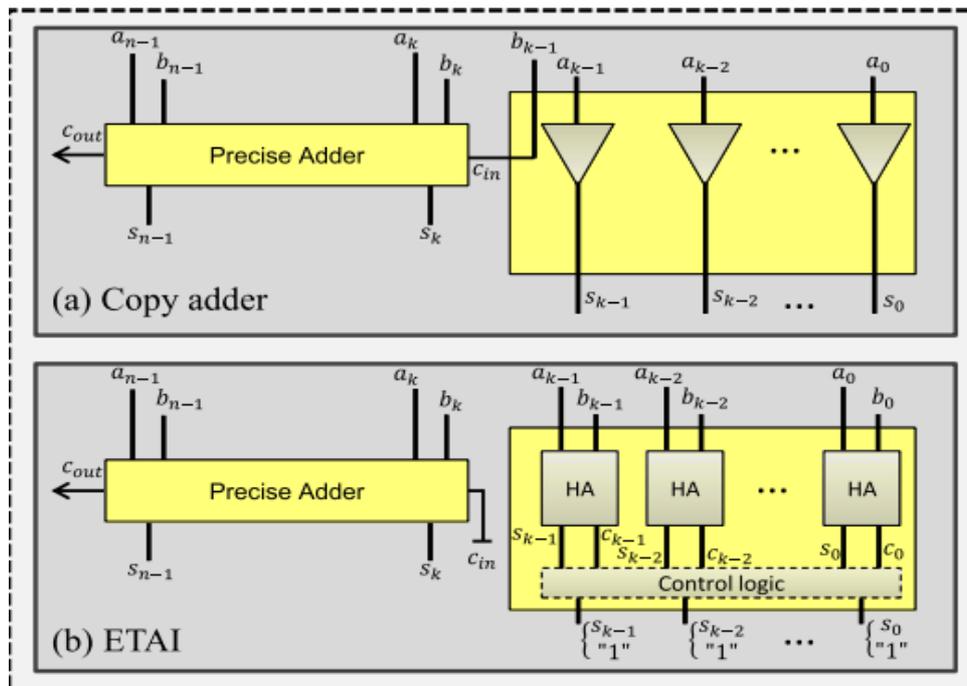


Fig. 1. Approximate adders: (a) Copy adder; (b) ETAI.

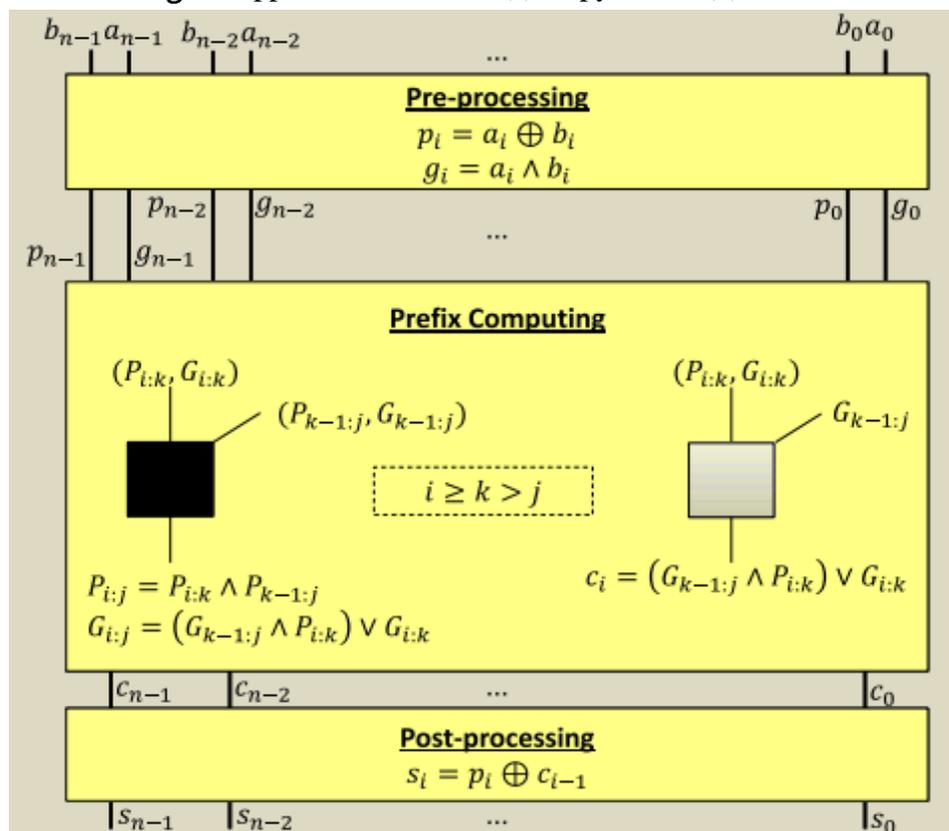


Fig. 2. Parallel prefix adder structure

The control logic block is conceived as follows: if the first carry-generate c is equal to “1,” then all the remaining least significant sum bits are set to “1.” Otherwise, the sum result is the one computed by the propagate signal. The carry-in to the precise part in ETAI is statically set to “0.” This procedure has 50% probability of getting the correct carry-in to the precise part. One can observe that for both the approximate adders, any conventional adder topology can be implemented in the precise part. In this work, we explore the

RCA, the high performance PPAs, and the low power adder fully optimized by the commercial tool used in this study. That is why in the next subsection a brief PPA overview is developed.

2.2. Precise Adders

As previously mentioned, adders are fundamental building blocks in a great variety of computational applications. Based on that, many adder topologies have been proposed to deal with the tradeoff between power and computational performance. The RCA topology is characterized to present low values of power consumption, area, and computational performance. Depending on the high-performance application requirements and given that computational complexity is increasing in nowadays tasks, the critical approach is to accelerate the adder's critical path delay (i.e. carry propagation) at the expense of higher area and power dissipation. Based on that, the Parallel Prefix Adders were proposed to deal with high-performance demands [24]. The carry propagation structure in the PPA adders is implemented by simple logic cells which tend to keep a regular connection. Based on that, the sum computation can be divided into pre-processing, prefix computation and post-processing parts, as can be seen in Figure 2. In the pre-processing part, the propagate p_i (i.e. $a_i \oplus b_i$) and generate g_i (i.e. $a_i \wedge b_i$) signals are computed based on the input operands a_i and b_i . In the prefix computation stage, the carry computation is accelerated by the parallel composition of the black cells which implement the group propagate $P_i: j$ and generate $G_i: j$ signals as well as the gray cells which compute the carry c_i . Finally, the post-processing step is given by the sum $s_i = p_i \oplus c_{i-1}$.

2.3 Drawbacks

At each stage of a carry-save addition,

1. We know the result of the addition at once.
2. We still do not know whether the result of the addition is larger or smaller than a given number (for instance, we do not know whether it is positive or negative).

3. PROPOSED METHOD

A. Preliminaries

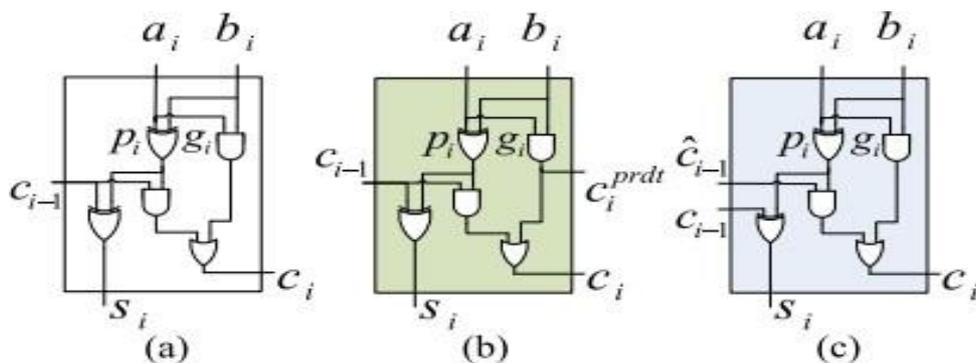


Fig. 3. Conventional full adder. (b) Carry-out selectable full adder. (c) Carry-in configurable full adder.

An N-bit adder operates on two addends $A = (a_N, a_{N-1}, \dots, a_i, \dots, a_1)$ and $B = (b_N, b_{N-1}, \dots, b_i, \dots, b_1)$. For bit i , its carry-in is c_{i-1} and its carry-out is c_i . Defining the carry generate bit $g_i = a_i \cdot b_i$, propagate bit $p_i = a_i \oplus b_i$, and kill bit $k_i = \bar{a}_i \cdot \bar{b}_i$, the conventional full adder computes the sum s_i and carry c_i according to

$$s_i = p_i \oplus c_{i-1} \quad (1)$$

$$c_i = g_i + p_i \cdot c_{i-1} \quad (2)$$

A gate level schematic of a conventional full adder is provided in Fig. 3(a). A CRA is used to chain N bits of conventional full adders together. By applying (2) recursively, one can get

$$c_i = g_i + p_i g_{i-1} + \dots + g_1 \quad i \geq 2 \quad p_k + c_0 \quad i \geq 1 \quad p_k \quad (3)$$

This equation implies that c_i can be computed directly from g and p of all bits, without waiting for the c of its

lower bits to be computed. This observation is the basis for CLA adder.

$$c_{prdt\ i} = g_i. \quad (4)$$

For the LSB of the higher bit subadder, which is bit $i + 1$, its carry-out c_{i+1} can be computed using one of two options: either by the conventional $c_{i+1} = g_{i+1} + p_{i+1} \cdot c_i$, or by using the carry prediction as

$$c_{i+1} = g_{i+1} + p_{i+1} \cdot c_{prdt\ i} = g_{i+1} + p_{i+1} \cdot g_i. \quad (5)$$

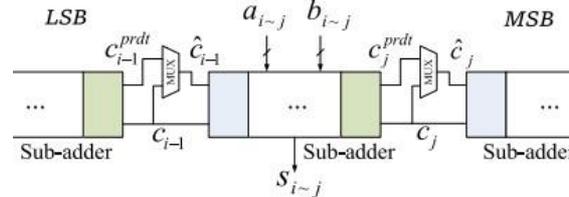


Fig. 4. Design of SARA

The selection between the two options is realized using MUXes as in Fig. 4 and the multiplexer (MUX) selection result is denoted as \hat{c}_i . Comparing (5) with (3), we can see that the carry prediction is a truncation-based approximation to carry computation. Therefore, \hat{c}_i can be configured to either accurate mode or approximation mode, that is $\hat{c}_i \leftarrow c_{prdt\ i}$, if approximation mode c_i , if accurate mode. (6)

It should be noted that the carry prediction $c_{prdt\ i}$ reuses g_i in an existing full adder instead of introducing an additional dedicated circuit as in [18] or Fig. 2. This prediction scheme makes a very simple modification to the conventional full adder, as shown in Fig. 3(b). One can connect \hat{c}_i to its higher bit $i + 1$ to compute both carry c_{i+1} and sum s_{i+1} , as in GDA [18] and RAP-CLA [19]. We suggest an improvement over this approach by another simple change as in Fig. 3(c), where s_{i+1} is based on c_i instead of \hat{c}_i . Such approach can help reduce the error rate in outputs when an incorrect carry is propagated. Because the sum keeps accurate and the carry will not be propagated when addends are exactly the same. Moreover, out of all four configurations of sum/carry calculation by approximate/accurate carry-in, the most meaningful way is to have sum bit calculated by accurate carry and make carry bit configurable.

Therefore, sum s_{i+1} is calculated directly by accurate carry c_i without the option of $c_{prdt\ i}$. Applying this in SARA as in Fig. 4, in the approximation mode, computing s_{j+1} from c_j can still limit the critical path to be between $c_{prdt\ i-1}$ and s_{j+1} , but has higher accuracy than computing s_{j+1} from \hat{c}_j . Compared to sum computation in GDA and RAP-CLA, this technique improves accuracy with almost no additional overhead. Compared to CRA, the overhead of SARA is merely the MUXes, which is almost the minimum possible for configurable adders. Although s_{j+1} is calculated by accurate carry c_j , its delay can still be reduced by approximate carry in lower subadder. In a multibit adder, the delay of sum bit depends on the carry chain propagated from its lower bits. In our SARA structure, even when accurate carry c_j is propagated at bit j , the carry chain might be truncated by approximate carry in other lower bits.

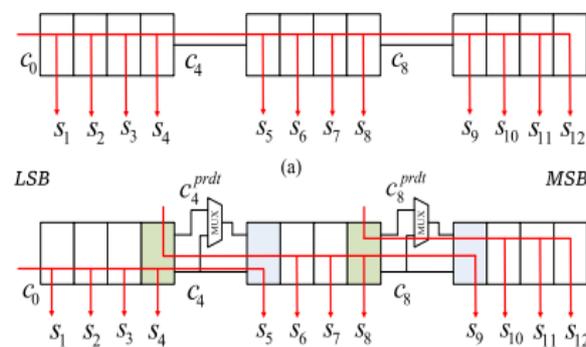


Fig. 5. Implementation of 12-bit adder in (a) CRA and (b) SARA

In Fig. 4, when $c_{prdt\ i-1}$ is propagated, the delay of s_{j+1} is reduced as its path is shortened to be between bit $i - 1$ and $j + 1$. We can take the 12-bit adder in Fig. 5 as an example. For 12-bit SARA working in approximate mode, the sum s_9 uses the accurate carry c_8 from a lower subadder (bits 5 to 8). But c_8 is propagated from approximate carry $c_{prdt\ 4}$ of another subadder (bits 1 to 4). As shown in the figure, the delay of s_9 in SARA is about six stages. Compared with the same bit in CRA, the delay of sum bit s_9 in SARA is reduced by three stages. Similar delay reduction can be observed in other sum bits (bits 6 to 12). For sums at bits 1 to 5, their delay is the same as CRA, because they are using an accurate carry c_0 from LSB. As a result, the maximum delay in 12-bit SARA is reduced, since for a multibit adder its maximum delay depends on the longest critical path.

4. SIMULATION RESULT

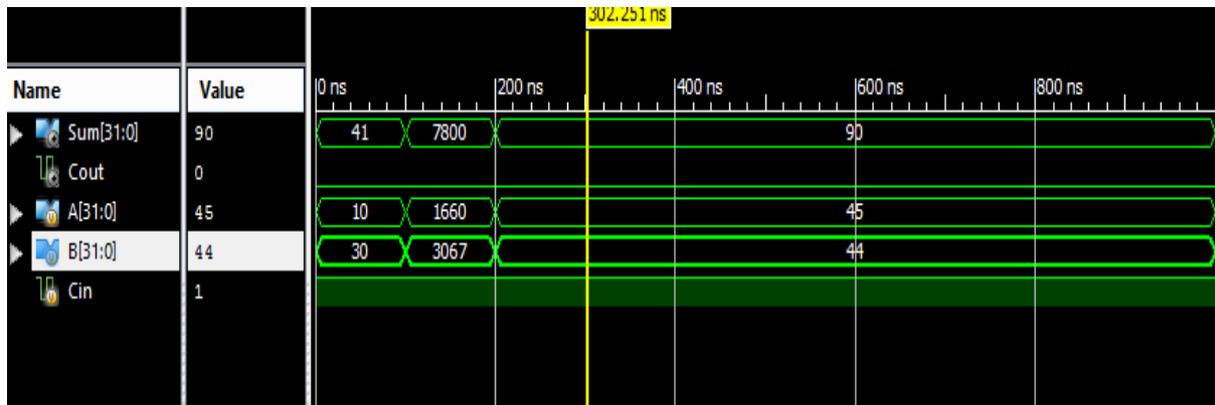


Fig. 6 existing simulation output

Device Utilization Summary (estimated values)			
Logic Utilization	Used	Available	Utilization
Number of Slice LUTs	79	17600	0%
Number of fully used LUT-FF pairs	0	79	0%
Number of bonded IOBs	98	100	98%

Fig. 7 Existing design summary

LUT3: I1->O	2	0.195	0.602	C1/r3/FA6/Cout1 (C1/r3/c6)
LUT3: I1->O	2	0.195	0.602	C1/r3/FA7/Cout1 (C1/r3/c7)
LUT3: I1->O	2	0.195	0.602	C1/r3/FA8/Cout1 (C1/Cout3)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA1/Cout1 (C1/r4/c1)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA2/Cout1 (C1/r4/c2)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA3/Cout1 (C1/r4/c3)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA4/Cout1 (C1/r4/c4)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA5/Cout1 (C1/r4/c5)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA6/Cout1 (C1/r4/c6)
LUT3: I1->O	2	0.195	0.602	C1/r4/FA7/Cout1 (C1/r4/c7)
LUT3: I1->O	1	0.195	0.360	C1/r4/FA8/Cout1 (Cout_OBUF)
OBUF: I->O	3.957			Cout_OBUF (Cout)
Total				30.199ns (10.967ns logic, 19.232ns route) (36.3% logic, 63.7% route)

Fig. 8 Existing time summary

A	B	C	D	E	F	G	H	I
Device			On-Chip	Power (W)	Used	Available	Utilization (%)	
Family	Virtex4		Logic	0.000	63	10944	1	
Part	xc4vfx12		Signals	0.000	132	---	---	
Package	ff668		DCMs	0.000	0	4	0	
Temp Grade	Commercial		IOs	0.000	97	320	30	
Process	Typical		Leakage	0.165				
Speed Grade	-10		Total	0.165				
Environment			Thermal Properties			Effective TJA (C/W)	Max Ambient (C)	Junction Temp (C)
Ambient Temp (C)	50.0					9.3	83.5	51.5
Use custom TJA?	No							
Custom TJA (C/W)	NA							
Airflow (LFM)	250							
Characterization								
PRODUCTION	v1.0.02-02-08							

Fig. 9 Existing power summary

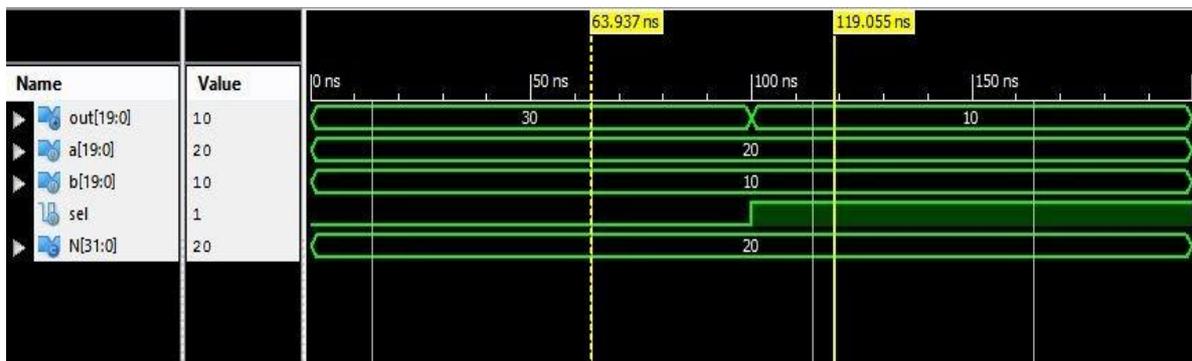


Fig. 10 Proposed simulation output

Device Utilization Summary (estimated values)			
Logic Utilization	Used	Available	Utilization
Number of Slices	36	5472	0%
Number of 4 input LUTs	63	10944	0%
Number of bonded IOBs	97	320	30%

Fig. 11 Proposed design summary

Component	Count	Logic Power (W)	Route Power (W)	Component Name
IBUF:I->O	5	0.000	0.561	a_1_IBUF (a_1_IBUF)
LUT6:I1->O	3	0.043	0.353	s1/s1/c4/Mxor_sout_xo<0>11 (s1/s1/c4/Mxor
LUT6:I4->O	3	0.043	0.353	s1/s2/c1/cout1 (s1/s2/c_t<0>)
LUT5:I3->O	3	0.043	0.353	s1/s2/c3/cout1 (s1/s2/c_t<2>)
LUT6:I4->O	3	0.043	0.353	s1/generate_N_bit_Adder[8].s3/c1/cout1 (s
LUT5:I3->O	3	0.043	0.353	s1/generate_N_bit_Adder[8].s3/c3/cout1 (s
LUT6:I4->O	3	0.043	0.353	s1/generate_N_bit_Adder[12].s3/c1/cout1
LUT5:I3->O	3	0.043	0.353	s1/generate_N_bit_Adder[12].s3/c3/cout1
LUT6:I4->O	3	0.043	0.353	s1/generate_N_bit_Adder[16].s3/c1/cout1
LUT5:I3->O	3	0.043	0.353	s1/generate_N_bit_Adder[16].s3/c3/cout1
LUT6:I4->O	3	0.043	0.353	s1/generate_N_bit_Adder[20].s3/c1/cout1
LUT5:I3->O	3	0.043	0.353	s1/generate_N_bit_Adder[20].s3/c3/cout1
LUT6:I4->O	3	0.043	0.353	s1/generate_N_bit_Adder[24].s3/c1/cout1
LUT5:I3->O	3	0.043	0.353	s1/generate_N_bit_Adder[24].s3/c3/cout1
LUT6:I4->O	3	0.043	0.353	s1/s4/c1/cout1 (s1/s4/c_t<0>)
LUT5:I3->O	2	0.043	0.433	s1/s4/c3/cout1 (s1/s4/c_t<2>)
LUT5:I2->O	1	0.043	0.279	Mmux_out261 (out_32_OBUF)
OBUF:I->O	0.000			out_32_OBUF (out<32>)
Total			6.904ns	(0.688ns logic, 6.216ns route)
				(10.0% logic, 90.0% route)

Fig. 12 Proposed time summary

A	B	C	D	E	F	G	H	I	J	K	L	M	N
Device		On-Chip	Power (W)	Used	Available	Utilization (%)		Supply	Summary	Total	Dynamic	Quiescent	
Family	Zynq-7000	Logic	0.000	66	17600	0		Source	Voltage	Current (A)	Current (A)	Current (A)	
Part	xc7z010	Signals	0.000	144	--	--		Vccint	1.000	0.006	0.000	0.005	
Package	clg400	I/Os	0.000	98	230	43		Vccaux	1.800	0.006	0.000	0.006	
Temp Grade	Commercial	Leakage	0.065					Vcco18	1.800	0.001	0.000	0.001	
Process	Typical	Total	0.065					Vccbram	1.000	0.000	0.000	0.000	
Speed Grade	-3							Vccpint	1.000	0.020	0.000	0.020	
								Vccpaux	1.800	0.013	0.000	0.013	
Environment		Thermal Properties	Effective TJA (C/W)	Max Ambient (C)	Junction Temp (C)			Vcco_dds	1.500	0.002	0.000	0.002	
Ambient Temp (C)	25.0		4.0	84.7	25.3								
Use custom TJA?	No												
Custom TJA (C/W)	NA												
Airflow (LFM)	250												
Heat Sink	Medium Profile												
Custom TSA (C/W)	NA												
Board Selection	Medium (10"x10")												
# of Board Layers	8 to 11												
Custom TJB (C/W)	NA												
Board Temperature (C)	NA												
								Supply Power (W)		Total	Dynamic	Quiescent	
										0.065	0.000	0.065	

Fig. 13 Proposed power summary

Table 1: comparison table

parameter	Existing	proposed
Number of slices	79	36
Time	30.199	6.904
Power	0.165	0.065

5. CONCLUSION

In this paper, we propose an SARA design. It has significantly lower power/EDP than the latest previous work when comparing at the same accuracy level. In addition, SARA has considerable lower area overhead than almost all the previous works. The accuracy-power-delay efficiency is further improved by a DAR technique. We demonstrate the efficiency of our adder in the applications of multiplication circuits and DCT computing circuits for image processing.

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